

$$\left. \begin{array}{l} 2x_1 - x_2 + 4x_3 + x_4 = 1 \\ 3x_1 + 2x_2 - 3x_3 + 2x_4 = 2 \\ -5x_1 + 3x_2 - x_3 + x_4 = 1 \end{array} \right\} \textcircled{2}$$

$$\begin{array}{c}
 \textcircled{2} \left\{ \begin{array}{l} 2x_1 - x_2 + 4x_3 + x_4 = 1 \\ 3x_1 + 2x_2 - 3x_3 + 2x_4 = 2 \\ \hline -5x_1 + 3x_2 - x_3 + x_4 = 1 \end{array} \right. \iff \begin{array}{c} \textcircled{5} \\[-3pt] \textcircled{-3} \end{array} \downarrow \\
 \left\{ \begin{array}{l} 2x_1 - x_2 + 4x_3 + x_4 = 1 \\ 6x_1 + 4x_2 - 6x_3 + 4x_4 = 4 \\ -10x_1 + 6x_2 - 2x_3 + 2x_4 = 2 \end{array} \right. \iff
 \end{array}$$

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$$\iff \updownarrow \left\{ \begin{array}{l} 2x_1 - x_2 + 4x_3 + x_4 = 1 \\ 7x_2 - 18x_3 + x_4 = 1 \\ x_2 + 18x_3 + 7x_4 = 7 \end{array} \right. \iff$$

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$$\iff \textcircled{\frac{-1}{48}} \left\{ \begin{array}{l} 2x_1 - x_2 + 4x_3 + x_4 = 1 \\ x_2 + 18x_3 + 7x_4 = 7 \\ -144x_3 - 48x_4 = -48 \end{array} \right.$$

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