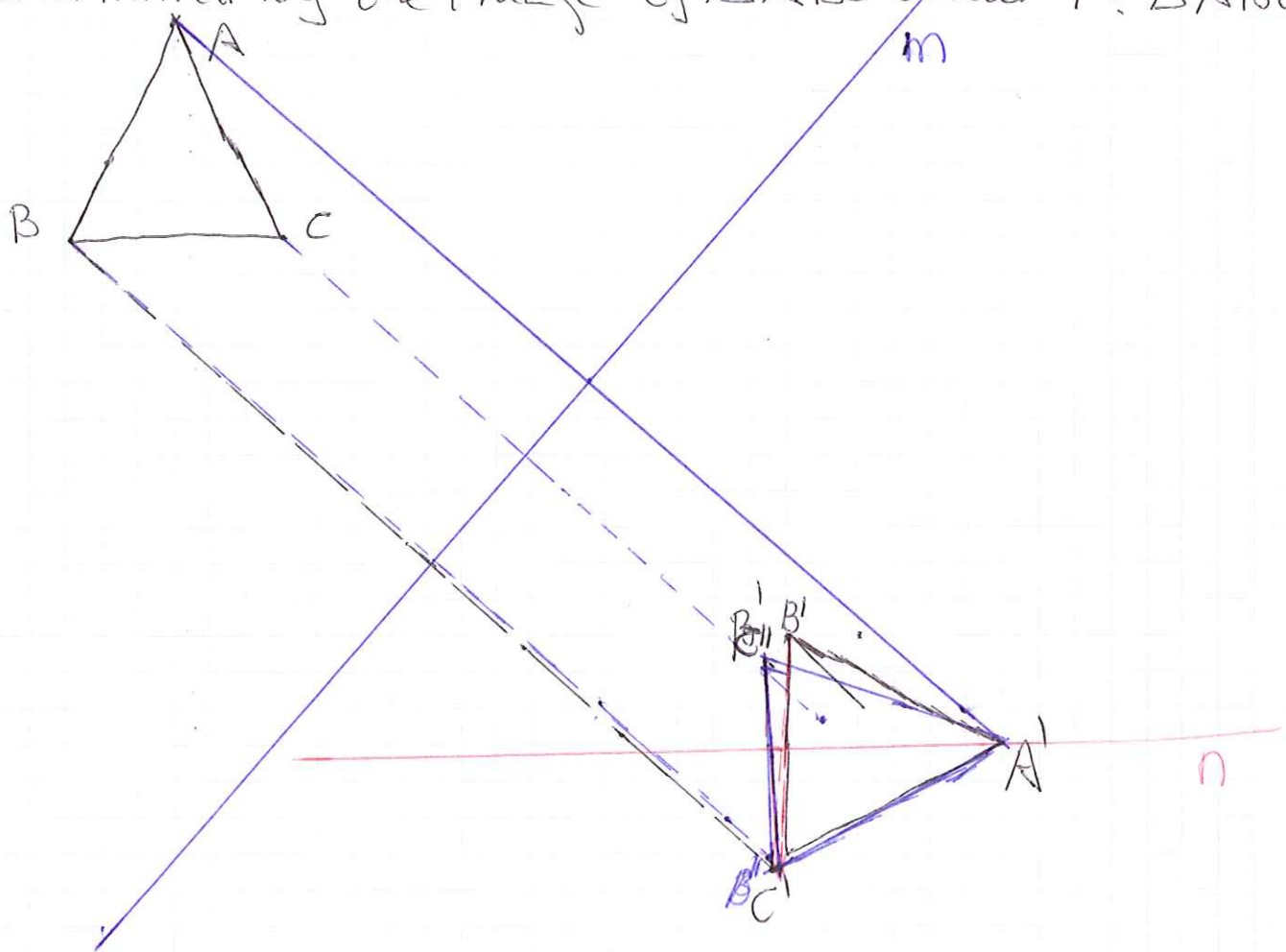


An isometry  $T$  is the product of at most three reflections.

We show here an example. We use that  $T$  is determined by the image of  $\triangle ABC$  under  $T$ :  $\triangle A'B'C'$



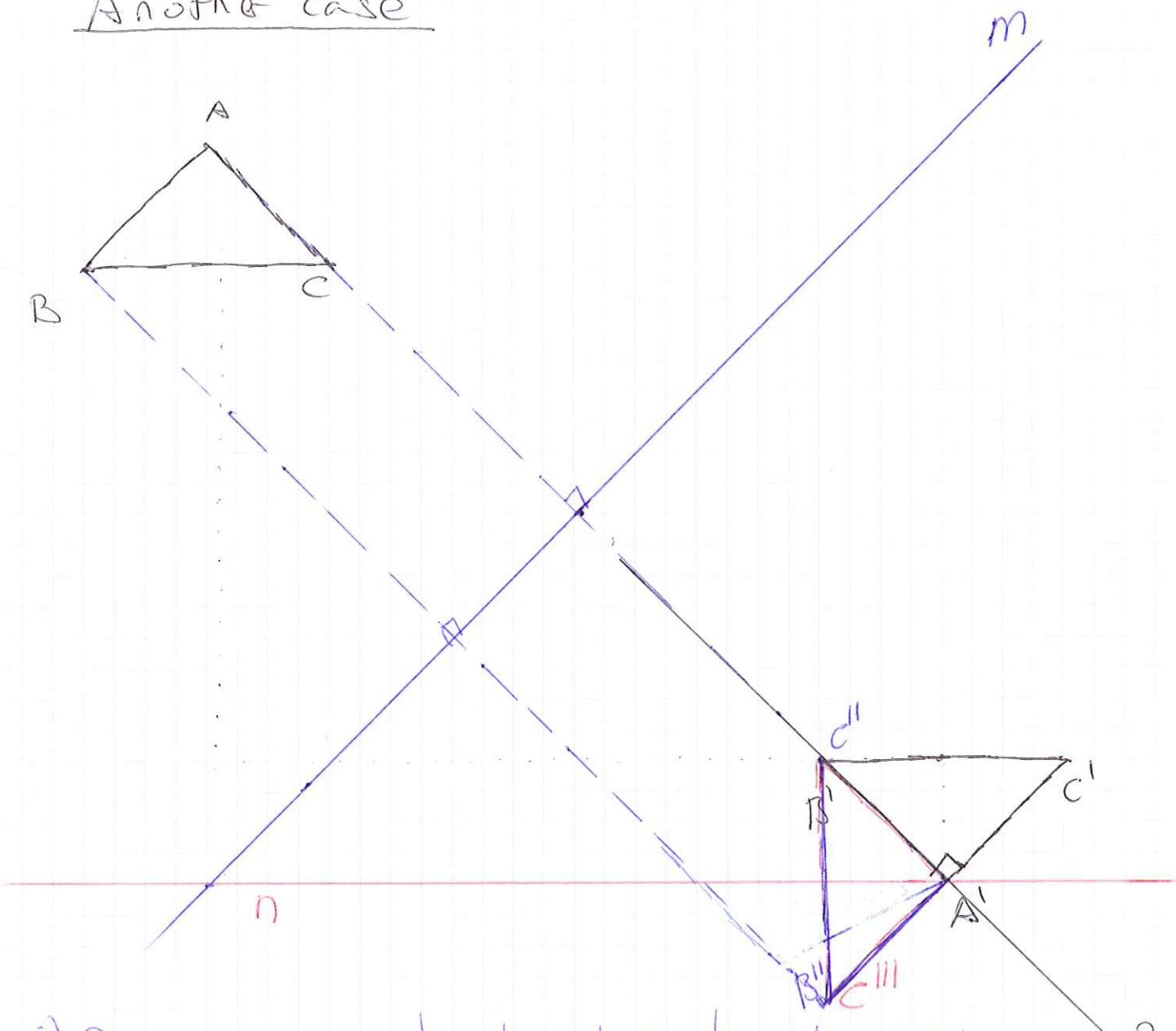
As  $A \neq A'$  we consider  $R_m$ , where  $m$  is the perpendicular bisector of  $AA'$ .  $R_m(\triangle ABC) = \triangle A'B''C''$

As  $B'' \neq B'$  still, consider  $R_n$ , where  $n$  is the perpendicular bisector of  $B''B'$ .  $R_n(\triangle A'B''C'') = \triangle A'B'C'$

Observe that in this case  $R_n(C'') = C'$  and

$$T = R_n R_m$$

## Another case



i)  $R_m$ ,  $m$  perpendicular bisector to  $AA'$   
 $R_m(\triangle ABC) = \triangle A'B''C''$  Observe  $B' \equiv C''$ , why not??

ii)  $R_n$ ,  $n$  perpendicular bisector to  $B''B'$   
 $R_n(\triangle A'B''C'') = \triangle A'B'C'''$ , where  $C''' \equiv B''$

iii)  $R_p$ ,  $p$  perpendicular bisector to  $C'''C'$  (observe this is the line  $B'A'$ )  $C'$  is the reflected point of  $C'''$  in  $p$  (observe also that  $A'$  is the midpoint between  $C'''$  and  $C'$ ) so  $R_p(\triangle A'B'C''') = \triangle A'B'C'$

$$\text{And } R_p R_n R_m(\triangle ABC) = \triangle A'B'C' = T(\triangle ABC)$$

$$T = R_p R_n R_m$$