

Exempel

Om $f(x, y) = x^2 + 2xy$, hur mycket ändras f ungefär om x ökar från 2 till 2.1 och y minskar från 3 till 2.8?

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Svar: Ökar ungefär med 0.2.