

Exempel

Bestäm differentialen till

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$$df = \frac{\partial f}{\partial x} dx + \frac{\partial f}{\partial y} dy + \frac{\partial f}{\partial z} dz$$

$$= (2x + z)dx - z \sin(yz)dy + (x - y \sin(yz))dz.$$