

Exempel

Rita mängden

$$\{(x, y) \in \mathbb{R}^2 : x < y, x^2 + 4y^2 \leq 4\}$$

samt beskriv dess inre punkter, yttra punkter samt randpunkter. Är mängden öppen, sluten eller varken eller?

Lösning

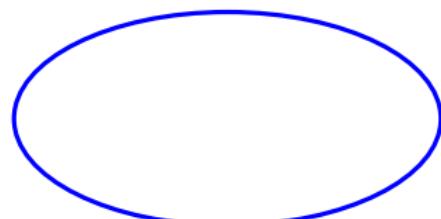
$$M = \{(x, y) \in \mathbb{R}^2 : x < y, x^2 + 4y^2 \leq 4\} = M_1 \cap M_2 \text{ där}$$

$$M_1 = \{(x, y) \in \mathbb{R}^2 : x < y\} \text{ och } M_2 = \{(x, y) \in \mathbb{R}^2 : x^2 + 4y^2 \leq 4\}.$$

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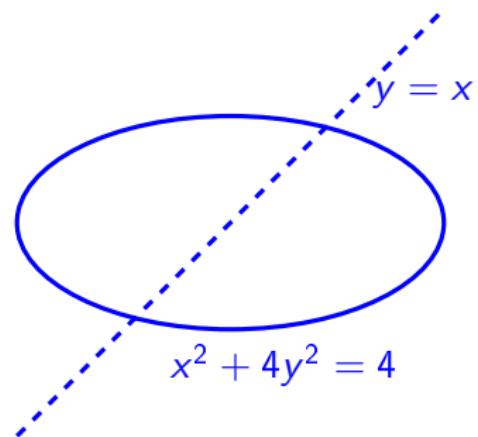


$$x^2 + 4y^2 = 4$$

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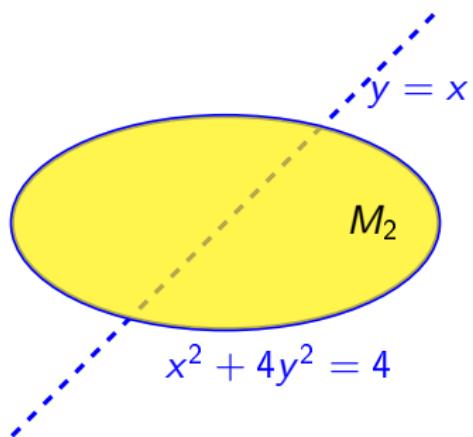
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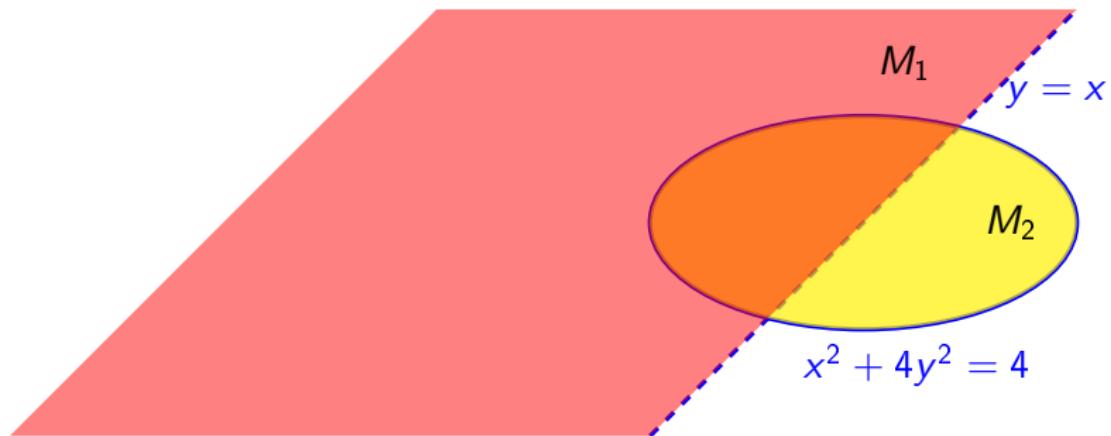
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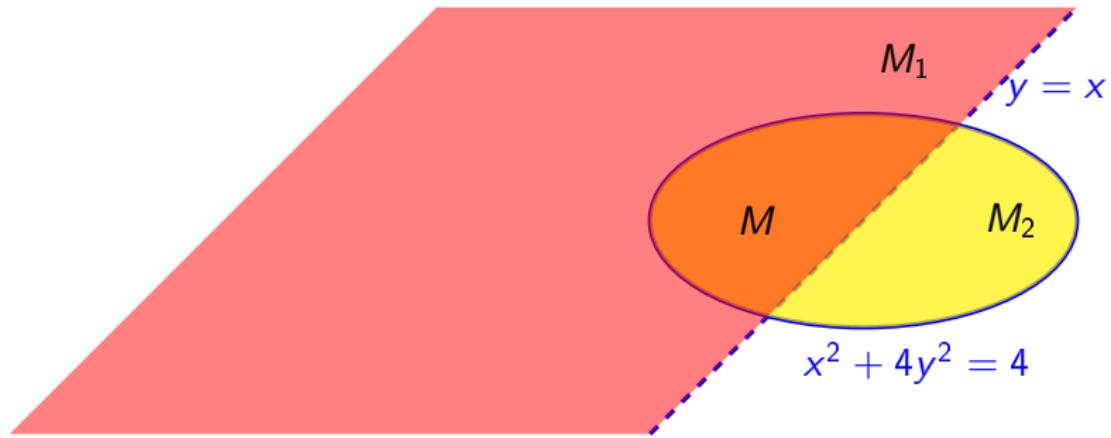
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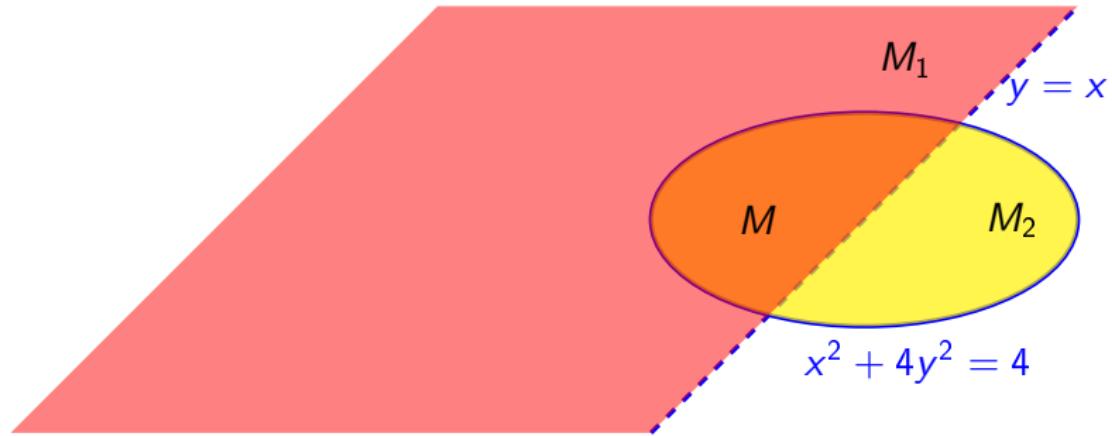


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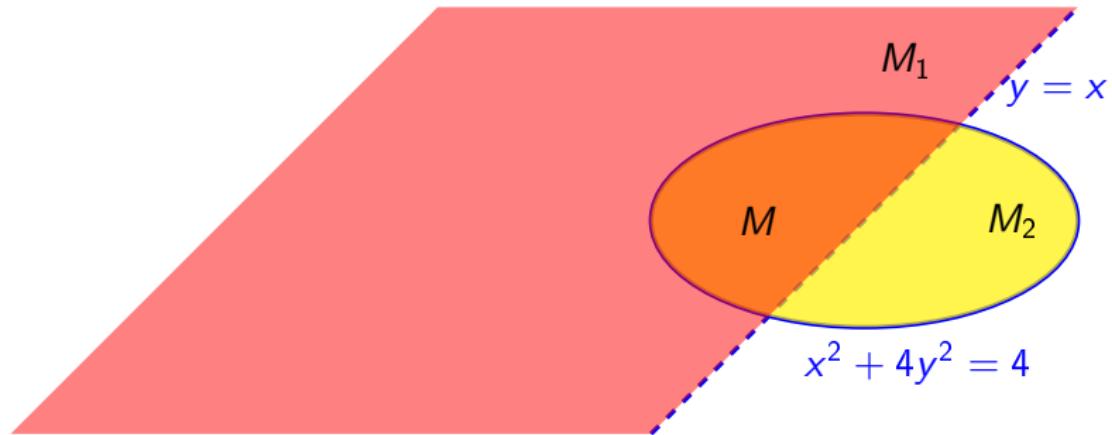
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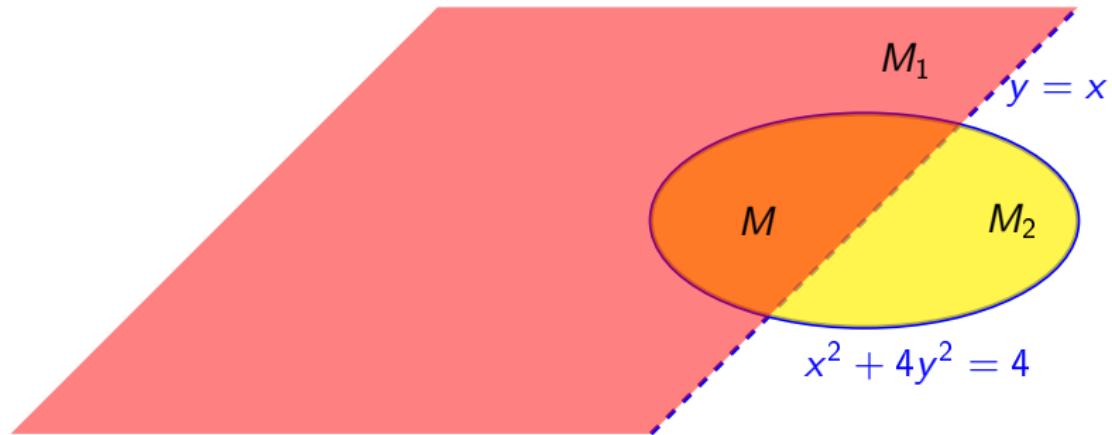


$$M^o = \{(x, y) \in \mathbb{R}^2 : x < y, x^2 + 4y^2 < 4\}.$$



$$M^\circ = \{(x, y) \in \mathbb{R}^2 : x < y, x^2 + 4y^2 < 4\}.$$

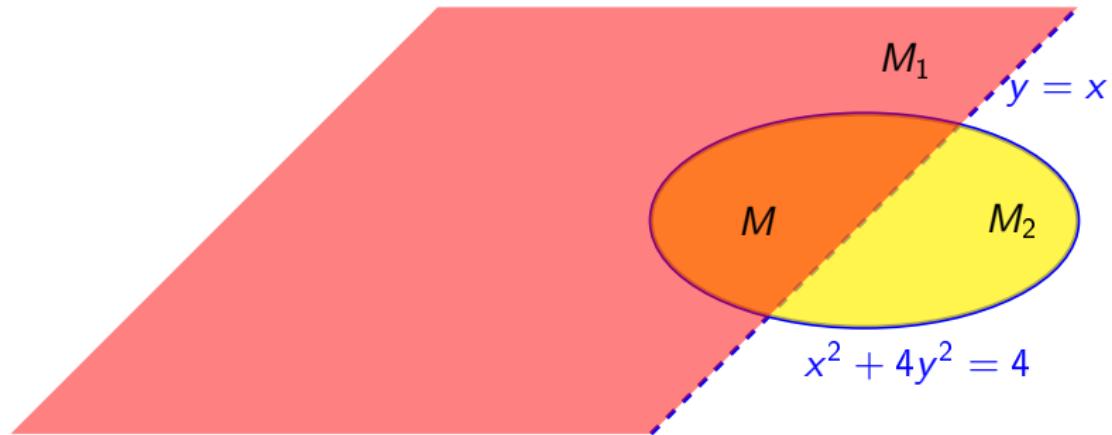
$$\partial M = \{(x, y) \in \mathbb{R}^2 : x < y, x^2 + 4y^2 = 4\} \cup \\ \{(x, y) \in \mathbb{R}^2 : x^2 + 4y^2 \leq 4, x = y\}.$$



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Yttre punkter: $\{(x, y) \in \mathbb{R}^2 : x > y\} \cup \{(x, y) \in \mathbb{R}^2 : x^2 + 4y^2 > 4\}$.



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M är varken öppen eller sluten.